# Estimating anti-retroviral treatment coverage using facility level data 

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## Estimating ART Coverage

- Reallocation model
- Crude solution to the problem
- Matches data from district to district
- Doesn't factor in where people live; size and location of facilities.
- Challenge lies in combining
- Number people living with HIV
- Number of people taking ART
- Choice of facilities (Distance, facility characteristics etc.)
- Probabilistic modelling



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- Choice in which facility to attend



## Motivating Example

- Choice in which facility to attend
- "Distance" to each facility


| Facility | A | B | C | D |
| :--- | :---: | :---: | :---: | :---: |
| Time | 19 | 18 | 21 | 43 |

## Motivating Example

- Choice in which facility to attend
- "Distance" to each facility
- Probability of attending facility $j$ from household $i$

$$
C_{j i} \propto \exp \left(-d_{j i}\right)
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- Distance is not the only factor influencing movement
- Probability of attending facility $j$ from household $i$

$$
C_{j i} \propto M_{j} \cdot \exp \left(-d_{j i}\right)
$$

- The number of people in household $i$ attending facility $j$ for ART with favourability

$$
C_{j i} \cdot \alpha_{i} \cdot \rho_{i} \cdot N_{i}
$$

| Sum across households to obtain the | Facility | A | B | C | D |  |
| :--- | :--- | :--- | :---: | :---: | :---: | :---: |
| number of patients attending facility. | Time | Probability | 0.32 | 18 | 21 | 0.33 |
|  | 0.28 | 43 |  |  |  |  |
|  | Probability | 0.21 | 0.21 | 0.18 | 0.40 |  |

## Modelling ART Coverage

- Estimate ART coverage using

$$
\hat{Y}_{i}^{A R T} \sim \operatorname{Bin}\left(\rho_{i} \cdot N_{i}, \alpha_{i}\right)
$$

- People move from moving to facility $j$ from region $i$ with probability $C_{j i}$
- Therefore we are observing

$$
Y_{j}^{A R T}=\sum_{i} C_{j i} \hat{Y}_{i}^{A R T}
$$

- How do we fit this in practice?
- Sum of a binomial is not a binomial
- How do we get the $C_{j i}$ (catchments)?


## Modelling ART Coverage

- ART coverage in region $i$ modelled as

$$
\hat{Y}_{i}^{A R T} \sim \operatorname{Poisson}\left(\rho_{i} \cdot N_{i} \cdot \alpha_{i}\right)
$$

- People move from region $j$ to facility $i$ with probability $C_{j i}$

$$
\begin{aligned}
& Y_{j}^{A R T}=\sum_{i} C_{j i} \hat{Y}_{i}^{A R T} \\
& Y_{j}^{A R T} \sim \operatorname{Poisson}\left(\sum_{i} C_{j i} \cdot \rho_{i} \cdot N_{i} \cdot \alpha_{i}\right)
\end{aligned}
$$

## Example: Malawi



Figure: (Left) Map of Traditional Authorities in South-eastern Malawi, (Center) Map of Facilities administering ART South-eastern Malawi and (Right) Travel time to nearest facility, by grid cell ( $1 \mathrm{~km} \cdot 1 \mathrm{~km}$ resolution).

- Prevalence
- HIVE
- Population-based HIV impact assessment survey (PHIA)
- Demographic and household surveys (DHS)
- Antenatal care facilities (ANC)
- Population
- worldpop
- Age and sex categorised
- Anti-retroviral therapy (ART)
- Travel times


Figure: (Left) Locations of facilities administering ART. (Right) Estimates of population, by grid cell $(1 \mathrm{~km} \cdot 1 \mathrm{~km}$ resolution).

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- Population of region $i$ - Fixed, obtained from worldpop


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- Population of region $i$ - Fixed, obtained from worldpop
- Prevalence of region $i$ - Fixed, obtained from HIVE
- ART coverage of region $i$ -

$$
\operatorname{logit}\left(\alpha_{i}\right) \sim N\left(0.7,0.3^{2}\right)
$$

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- Catchment probabilities from region $i$ to facility $i$ -

$$
C_{j i} \propto M_{j} \cdot \kappa\left(d_{j i}\right)
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- $d_{j i}$ average distance from region $j$ to facility $i$


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- Kernel controlling the

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\kappa(x)=\exp (-x)
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- 'Favourability' factor

$$
\log \left(M_{j}\right)=\beta_{0 j}+\sum_{k} \beta_{k} X_{j k}
$$

## Results



Figure: Estimated ART coverage under different scales of the kernels.

## Results



Figure: Probability of attending Bangwe Health Centre in Blantyre under different scales of the kernels.

## Results



Figure: Estimated ART coverage with altered prior on the ART coverage.

## Summary and Future Work

- Produced a model that estimates
- ART coverage
- Probabilistic catchments
- Future work
- Incorporate other sources of data?
- Other types of catchment?

Any Questions？


