### Estimating anti-retroviral treatment coverage using facility level data

Matthew Thomas

Imperial College London

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### ESTIMATING ART COVERAGE

#### Reallocation model

- Crude solution to the problem
- Matches data from district to district
- Doesn't factor in where people live; size and location of facilities.
- Challenge lies in combining
  - Number people living with HIV
  - Number of people taking ART
  - Choice of facilities (Distance, facility characteristics etc.)
- Probabilistic modelling



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#### A household

- ▶ *N<sub>i</sub>* individuals
- *ρ<sub>i</sub>* prevalence
   *α<sub>i</sub>* probability of receiving ART



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- A household
  - ▶ N<sub>i</sub> individuals
  - $\triangleright \rho_i$  prevalence
  - $\alpha_i$  probability of receiving ART
- Mean number of people receiving ART is given by

$$\alpha_i \cdot \rho_i \cdot N_i$$





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Choice in which facility to attend



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- Choice in which facility to attend
- "Distance" to each facility



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- Choice in which facility to attend
- "Distance" to each facility
- Probability of attending facility *j* from household *i*

 $C_{ji} \propto exp(-d_{ji})$ 



Facility	Α	В	С	D
Time	19	18	21	43
Probability	0.32	0.33	0.28	0.06

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 Distance is not the only factor influencing movement



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- Distance is not the only factor influencing movement
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 $C_{ji} \propto M_j \cdot exp(-d_{ji})$ 

The number of people in household *i* attending facility *j* for ART with favourability

$$C_{ji} \cdot \alpha_i \cdot \rho_i \cdot N_i$$

 Sum across households to obtain the number of patients attending facility.



Facility	Α	В	С	D
Time	19	18	21	43
Probability	0.32	0.33	0.28	0.06
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Estimate ART coverage using

$$\hat{Y}_i^{ART} \sim Bin(\rho_i \cdot N_i, \alpha_i)$$

- People move from moving to facility j from region i with probability C<sub>ji</sub>
- Therefore we are observing

$$Y_j^{ART} = \sum_i C_{ji} \hat{Y}_i^{ART}$$

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- How do we fit this in practice?
  - Sum of a binomial is not a binomial
  - ▶ How do we get the *C*<sub>*ji*</sub> (catchments)?

ART coverage in region *i* modelled as

$$\hat{Y}_{i}^{ART} \sim Poisson(\rho_{i} \cdot N_{i} \cdot \alpha_{i})$$

People move from region *j* to facility *i* with probability C<sub>ji</sub>

$$\begin{split} Y_{j}^{ART} &= \sum_{i} C_{ji} \hat{Y}_{i}^{ART} \\ Y_{j}^{ART} &\sim \textit{Poisson}\left(\sum_{i} C_{ji} \cdot \rho_{i} \cdot N_{i} \cdot \alpha_{i}\right) \end{split}$$

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### EXAMPLE: MALAWI



Figure: (Left) Map of Traditional Authorities in South-eastern Malawi, (Center) Map of Facilities administering ART South-eastern Malawi and (Right) Travel time to nearest facility, by grid cell (1km · 1km resolution).

### Data

### Prevalence

- ► HIVE
- Population-based HIV impact assessment survey (PHIA)
- Demographic and household surveys (DHS)
- Antenatal care facilities (ANC)
- Population
  - worldpop
  - Age and sex categorised
- Anti-retroviral therapy (ART)
- Travel times



Figure: (Left) Locations of facilities administering ART. (Right) Estimates of population, by grid cell (1km · 1km resolution).

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$$Y_j^{ART} \sim Poisson\left(\sum_i C_{ji} \cdot \rho_i \cdot \mathbf{N}_i \cdot \alpha_i\right)$$

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Population of region *i* - Fixed, obtained from worldpop

$$Y_j^{ART} \sim Poisson\left(\sum_i C_{ji} \cdot \boldsymbol{\rho}_i \cdot N_i \cdot \alpha_i\right)$$

- Population of region *i* Fixed, obtained from worldpop
- **Prevalence of region** *i* Fixed, obtained from HIVE

$$Y_j^{ART} \sim Poisson\left(\sum_i C_{ji} \cdot \rho_i \cdot N_i \cdot {oldsymbol lpha}_i
ight)$$

- Population of region *i* Fixed, obtained from worldpop
- Prevalence of region *i* Fixed, obtained from HIVE
- ART coverage of region *i* -

$$\operatorname{logit}(\alpha_i) \sim N(0.7, 0.3^2)$$

$$Y_j^{ART} \sim Poisson\left(\sum_i \mathbf{C}_{ji} \cdot \rho_i \cdot N_i \cdot \alpha_i\right)$$

Catchment probabilities from region *i* to facility *i* -

 $C_{ji} \propto M_j \cdot \kappa(d_{ji})$ 

$$Y_j^{ART} \sim Poisson\left(\sum_i C_{ji} \cdot \rho_i \cdot N_i \cdot \alpha_i\right)$$

Catchment probabilities from region *i* to facility *i* -

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*d<sub>ji</sub>* average distance from region *j* to facility *i* 

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Catchment probabilities from region *i* to facility *i* -

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*d<sub>ji</sub>* average distance from region *j* to facility *i* Kernel controlling the

 $\kappa(x) = \exp(-x)$ 

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$$Y_j^{ART} \sim Poisson\left(\sum_i C_{ji} \cdot \rho_i \cdot N_i \cdot \alpha_i\right)$$

Catchment probabilities from region *i* to facility *i* -

 $C_{ji} \propto \mathbf{M}_j \cdot \kappa(d_{ji})$ 

*d<sub>ji</sub>* average distance from region *j* to facility *i*

Kernel controlling the

$$\kappa(x) = \exp(-x)$$

'Favourability' factor

$$log(M_j) = \beta_{0j} + \sum_k \beta_k X_{jk}$$

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## RESULTS



Figure: Estimated ART coverage under different scales of the kernels.

RESULTS



Figure: Probability of attending Bangwe Health Centre in Blantyre under different scales of the kernels.

RESULTS



Figure: Estimated ART coverage with altered prior on the ART coverage.

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## SUMMARY AND FUTURE WORK

- Produced a model that estimates

  - ART coverageProbabilistic catchments
- Future work
  - Incorporate other sources of data?

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Other types of catchment?

# ANY QUESTIONS?



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